



Solar System Ephemerides, Pulsar Timing, and Navigation

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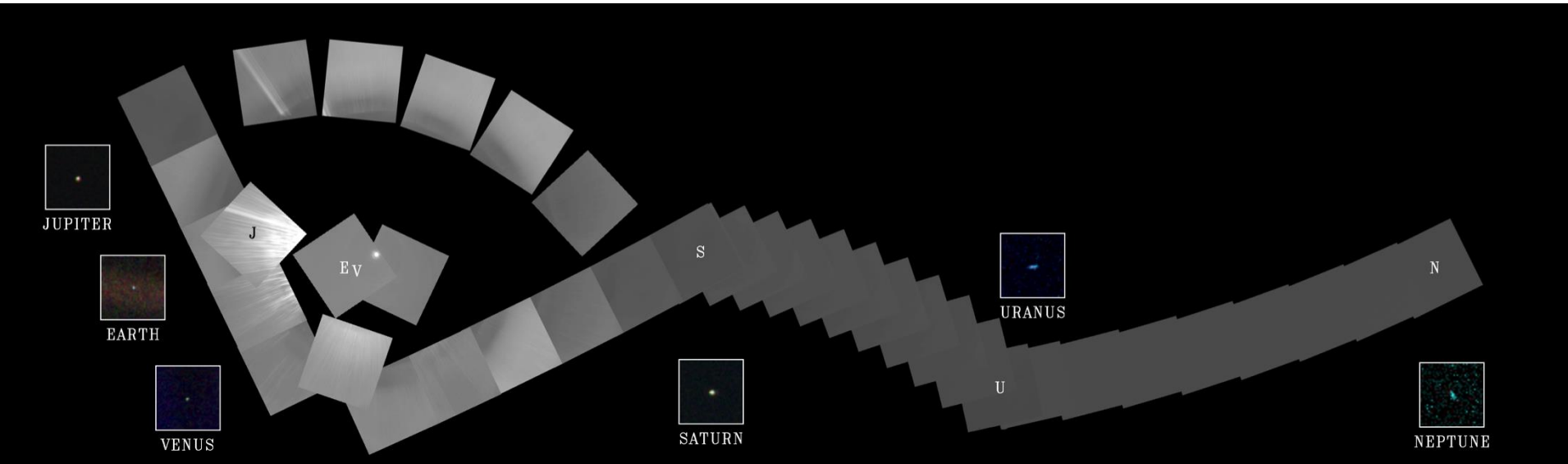


Jet Propulsion Laboratory
California Institute of Technology

Part I: The Solar System Ephemeris

Voyager's Family Portrait

a.k.a. The Solar System



Voyager 1 spacecraft at edge of our solar system (1990 February 14)

- Mars obscured by scattered light in camera (“rays of light”)
- Mercury too close to the Sun

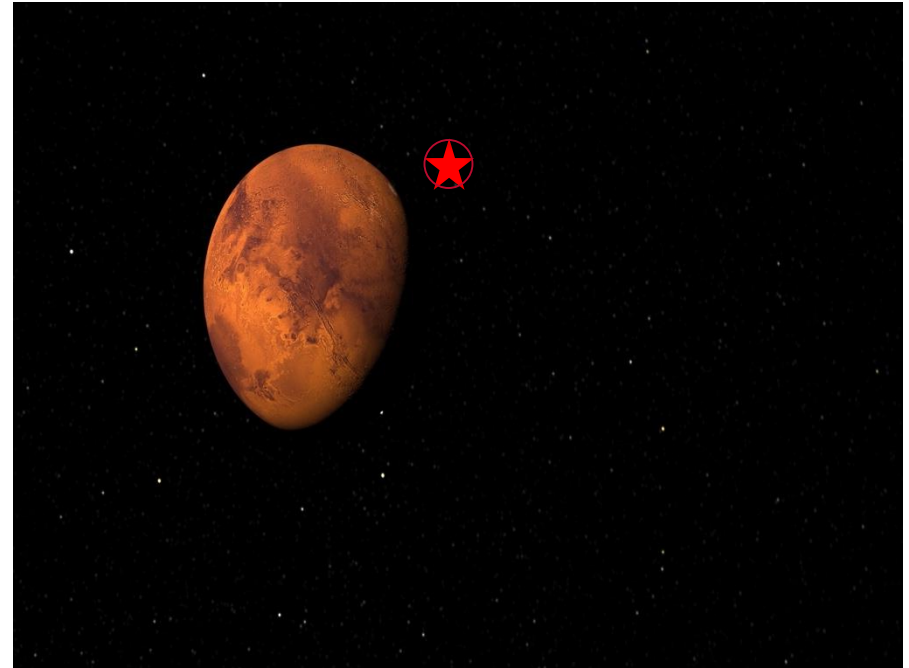
Credit: NASA/JPL

Spacecraft Navigation

Objective: Ensure spacecraft reaches required **aimpoint**

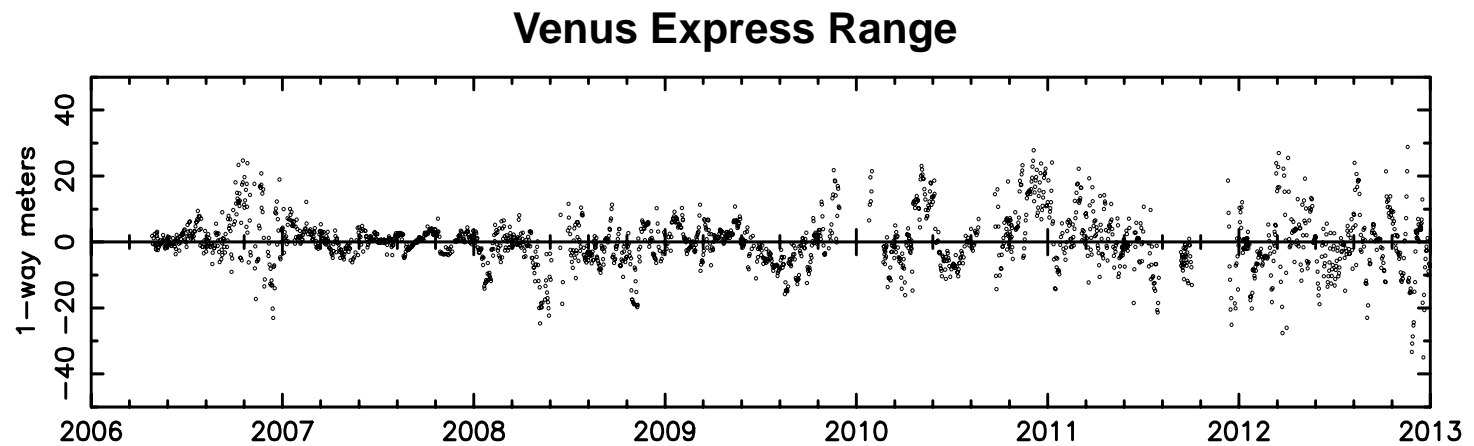
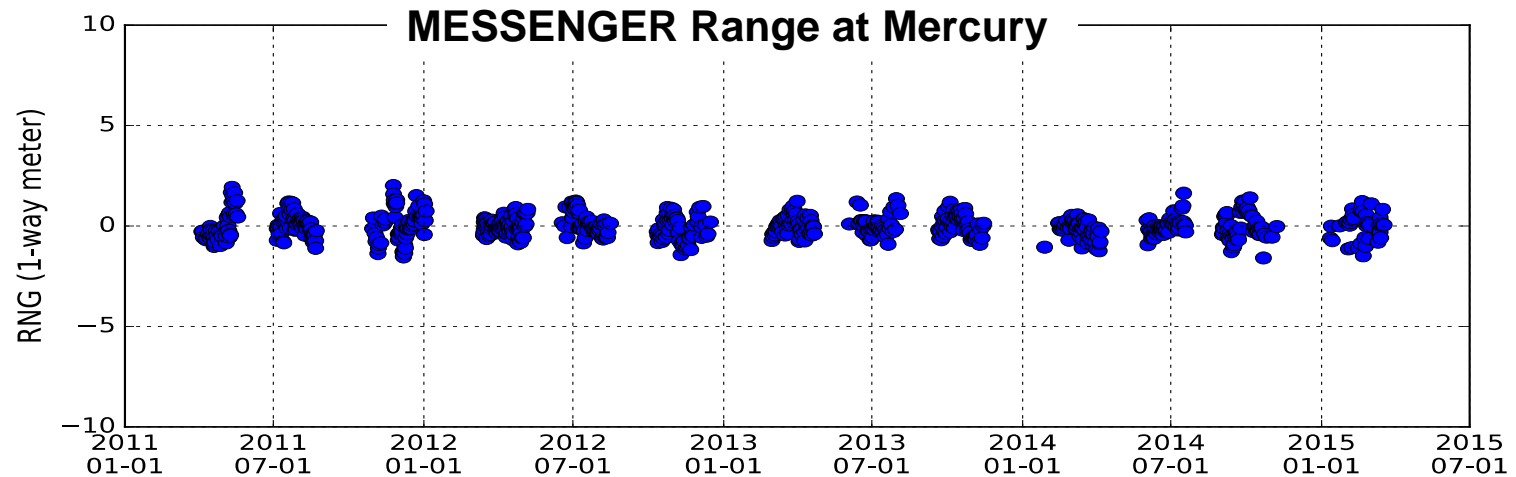
Requirements:

- Mars landing: 100 m accuracy [top of atmosphere]
winds ~ 1 m/s
 - Other body landing: > 100 m accuracy (?)
Propulsion, terrain relative navigation
 - Orbit insertion: ≥ 1000 m accuracy
- **Aimpoint = state vector: $(x, y, z; v_x, v_y, v_z)$**



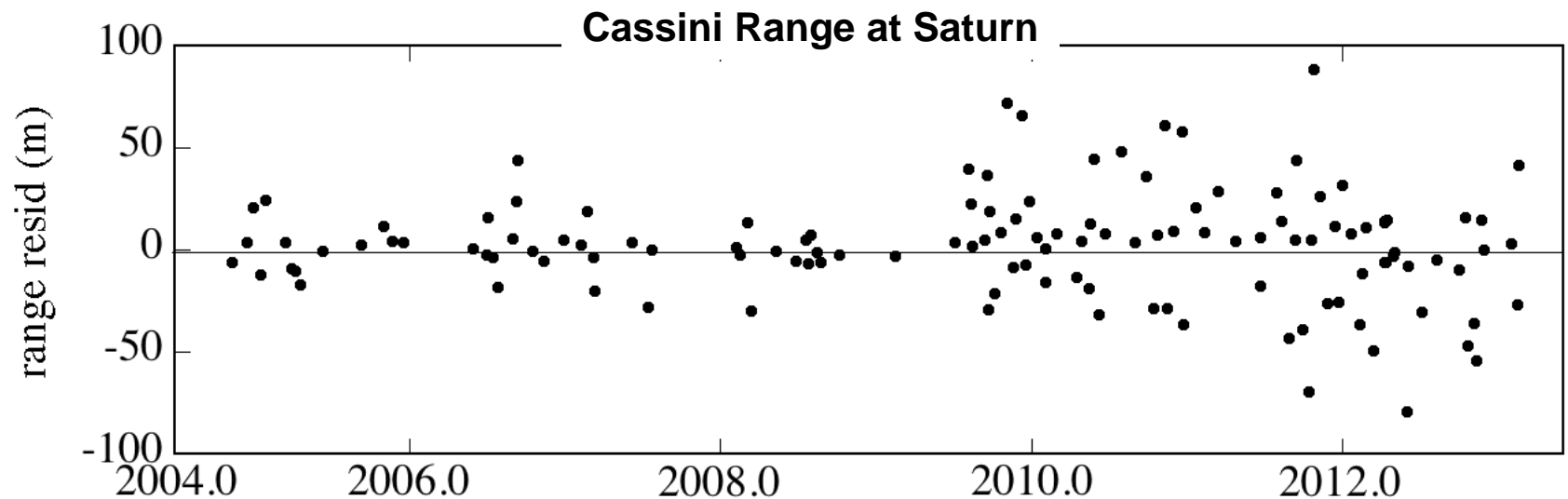
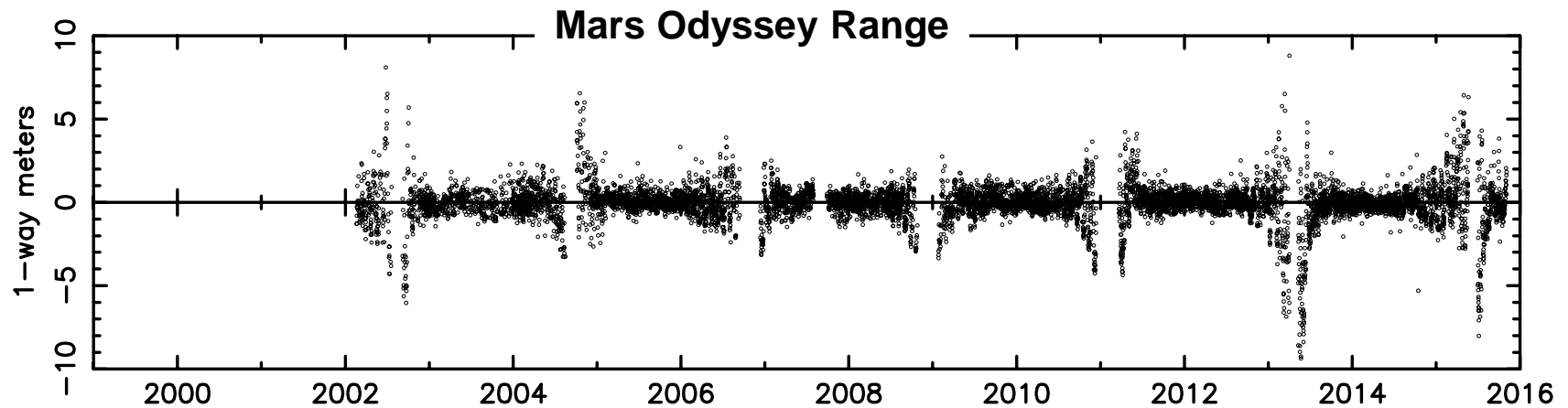
B-plane is normal to approach trajectory
Aimpoint at top of Mars' atmosphere is targeted to ensure accurate landing on surface

Mercury and Venus Data



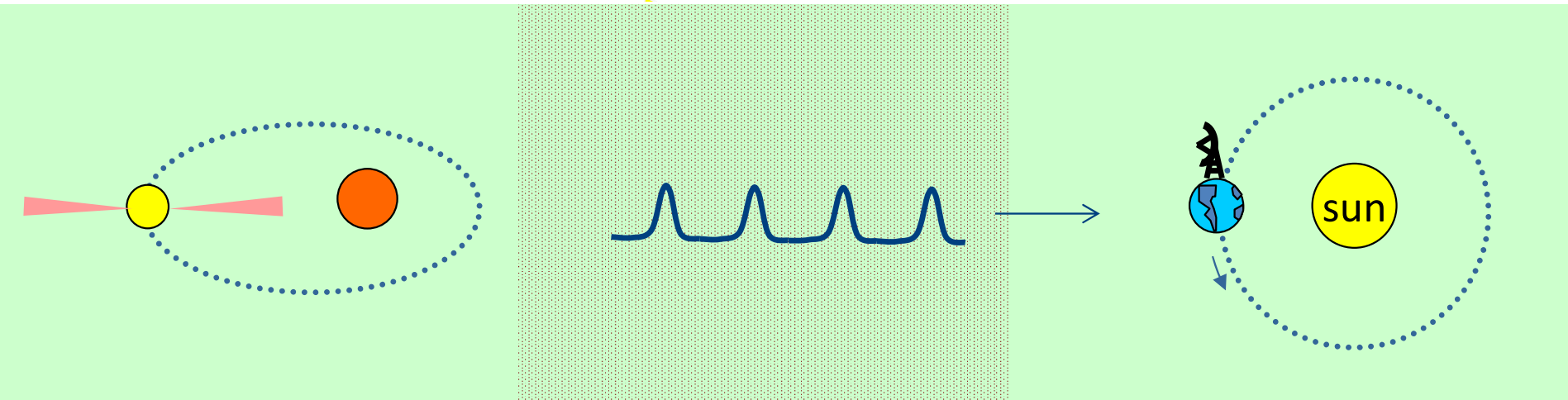
W. Folkner,
R. Park

Mars and Saturn Range



Part II: The Solar System Ephemeris and Pulsar Timing

Pulsar Timing and Solar System Ephemeris



$$t_{\text{SSB}} = t_{\text{topo}} + t_{\text{corr}} - DDM/v^2 + \Delta_{\text{R}\odot} + \Delta_{\text{S}\odot} + \Delta_{\text{E}\odot}$$

Lorimer & Kramer, eqn. (8.6)

$$\Delta_{\text{R}\odot} = -\mathbf{r} \cdot \hat{\mathbf{s}}/c$$

Lorimer & Kramer, eqn. (8.7)

Solar System Ephemeris

What Do We Want?

$$\sigma_{\text{TOA}} = \sigma_{\text{GWB}} + \sigma_{\text{SSB}} + \sigma_{\text{jitter}} + \sigma_{\Delta\text{DM}} + \dots + \sigma_{\text{random}}$$

$$\sigma_{\text{GWB}} \sim 10 \text{ ns}$$

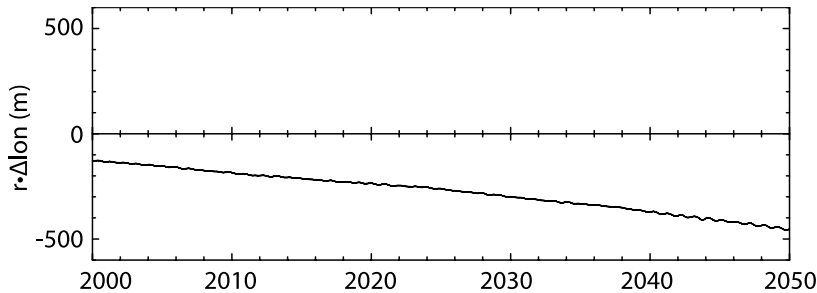
**[reasonable expectation based on current astrophysics
uncertainties]**

$$\sigma_{\text{SSB}} \sim \sigma_{\text{GWB}}/3 \sim 3 \text{ ns} \sim 1 \text{ m}$$

[cf. 100 m ~ 300 ns]

➤ **See also S. Taylor's talk.**

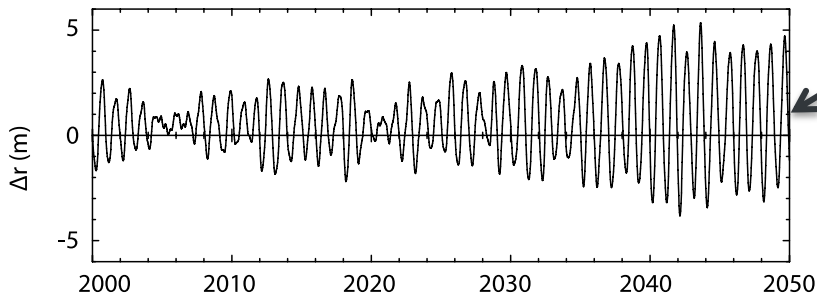
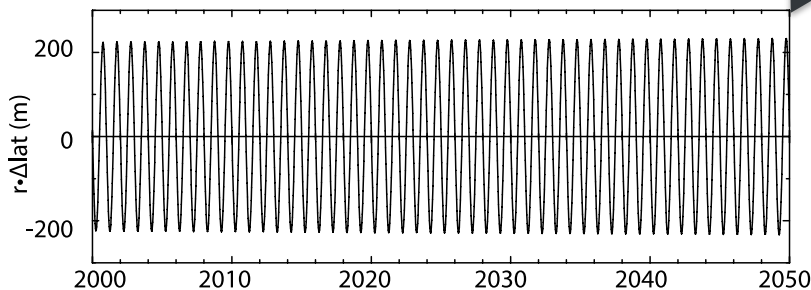
Earth relative to Sun, DE421 – DE430



Change in ecliptic longitude at 2000.0 and variation in latitude reflect VLBI accuracy.

$1 \text{ au} \cdot 0.3 \text{ mas} \sim 200 \text{ m}$

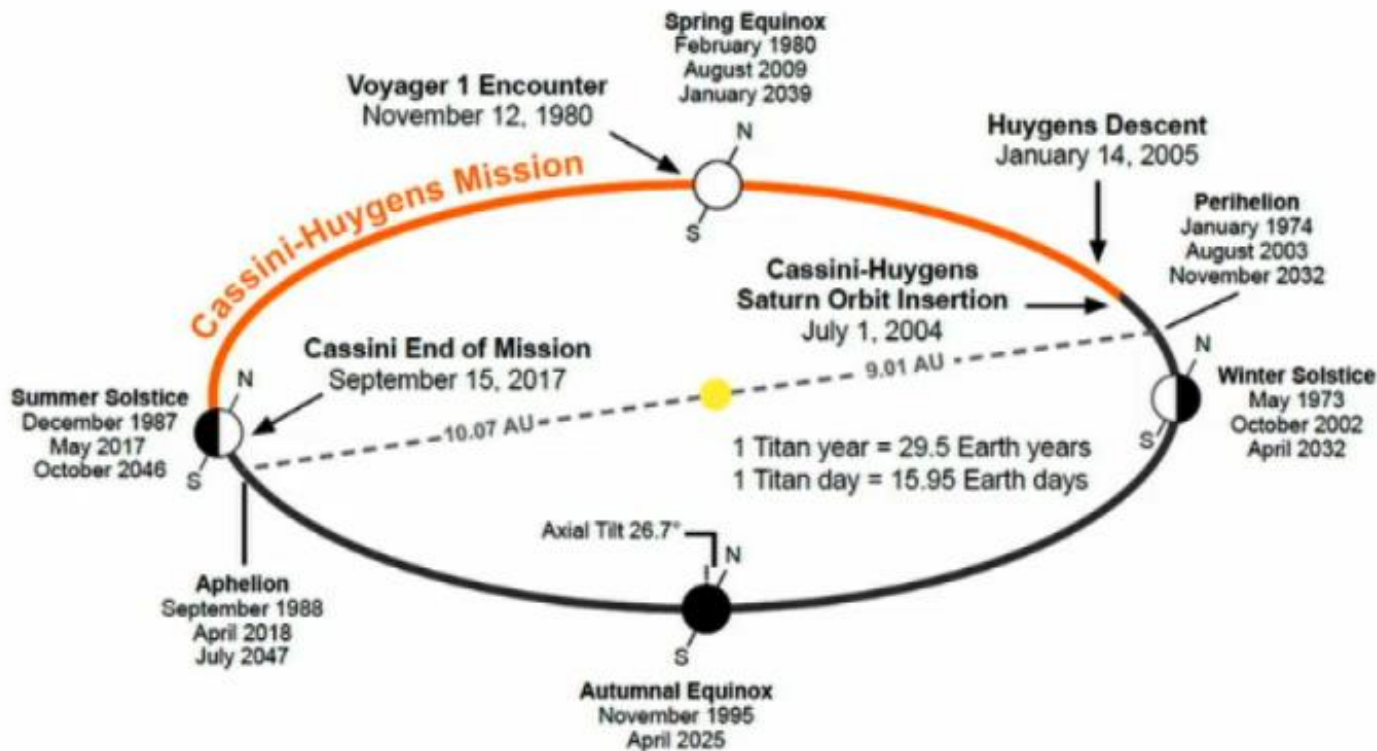
Earth-Sun distance stable to $\sim 5 \text{ m}$



W. Folkner, R. Park

Outer Planets

Large Mass, Long Lever Arm, Little Data



cf. timing model for PSR J1024-0719

Hörst 2017

Spacecraft Navigation and Solar System Ephemeris

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Requirements

- Mars landing: 100 m accuracy [top of atmosphere]
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- Other body landing: > 100 m accuracy (?)

Propulsion, terrain relative navigation

- Orbit insertion: ≥ 1000 m accuracy

➤ **Might know more later in August**



**B-plane is normal to approach trajectory
Aimpoint at top of Mars' atmosphere is targeted to ensure accurate landing on surface**

Pulsar Timing and Solar System Ephemeris

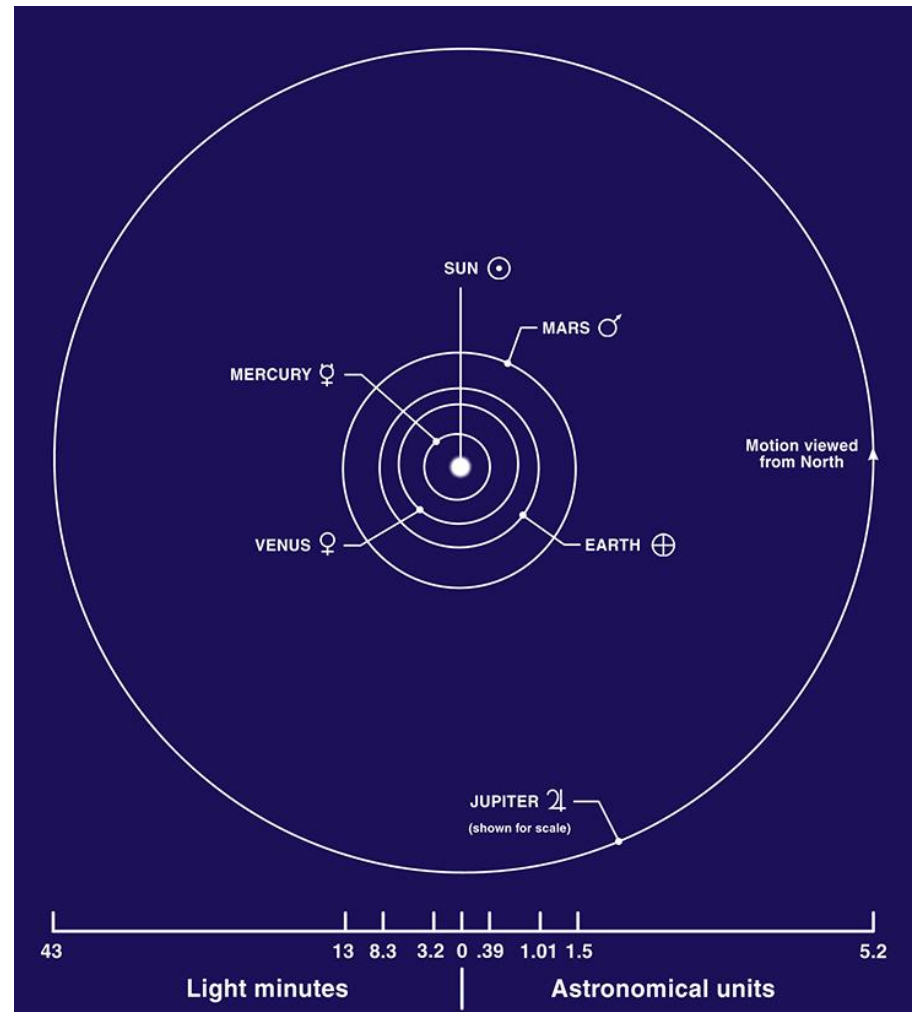
Or, Why Bother with the Spacecraft People?

**Make a pulsar-based
solar system
ephemeris?**

- cf. IPTA solar system project

Challenge: Enough good pulsars?

Best pulsars for
constructing frame are
best for GW study ...



Part III: Navigation

Pulsar Navigation?

TDA Progress Report 42-63

March and April 1981

The Telecommunications and Data Acquisition Progress Report

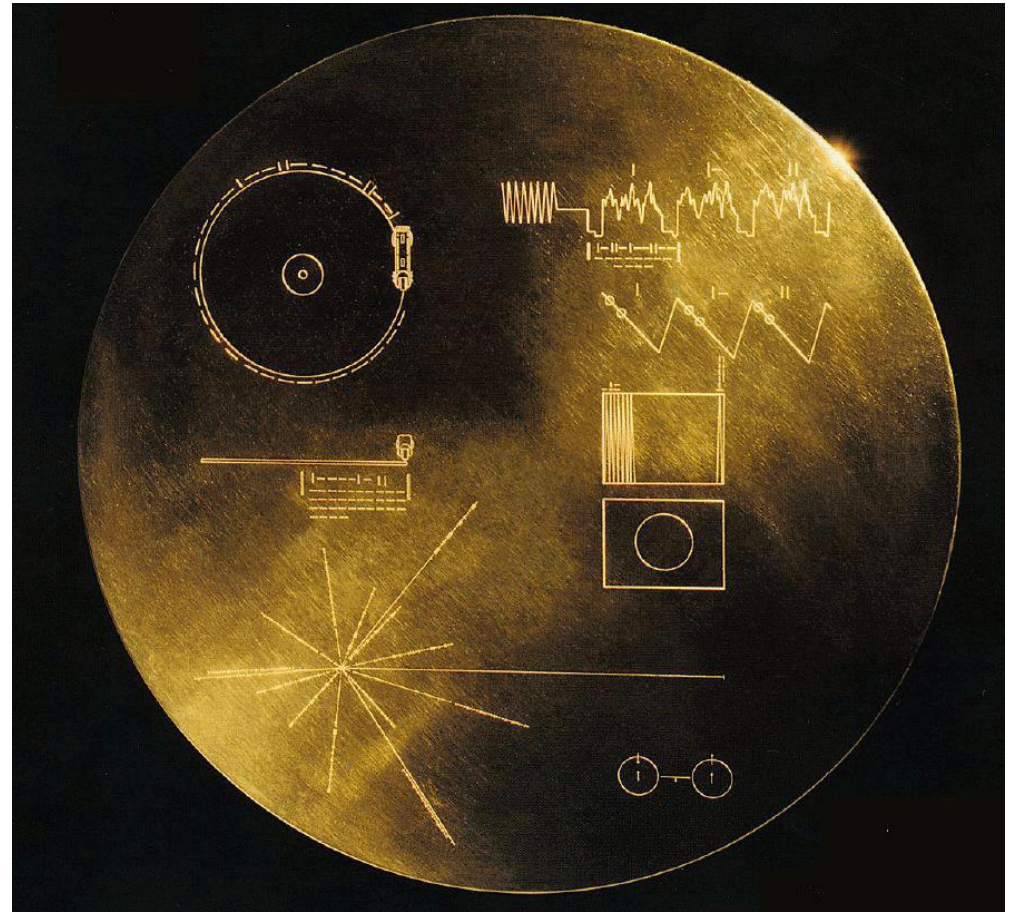
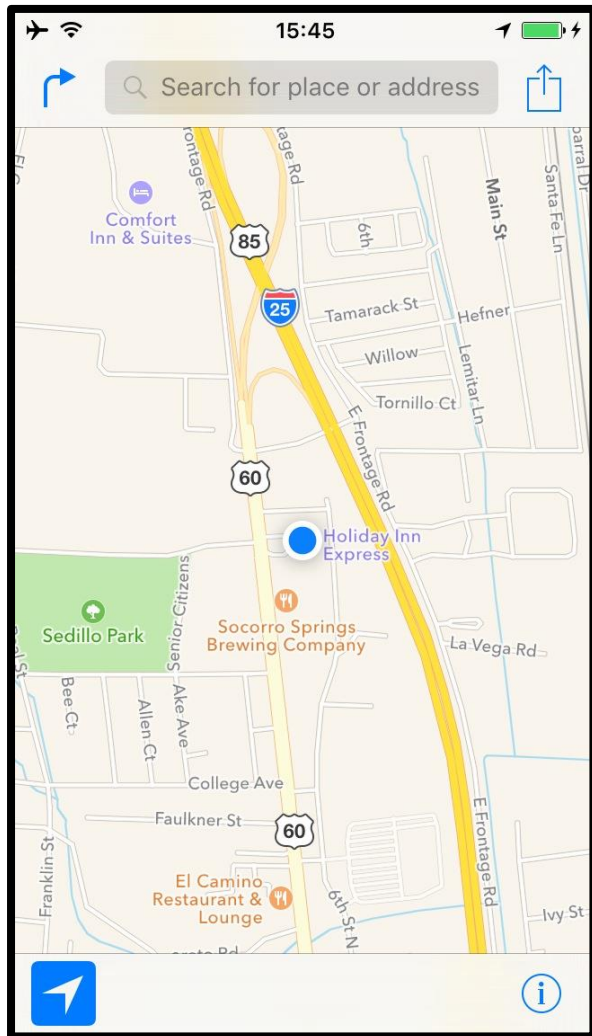
Navigation Using X-Ray Pulsars

T. J. Chester and S. A. Butman
Communications Systems Research Section

Approximately one-dozen X-ray pulsars are presently known which emit strong stable pulses with periods of 0.7 to ~ 1000 s. By comparing the arrival times of these pulses at a spacecraft and at the Earth (via an Earth-orbiting satellite), a three-dimensional position of the spacecraft can be determined. One day of data from a small ($\sim 0.1 \text{ m}^2$) on-board X-ray detector yields a three-dimensional position accurate to ~ 150 km. This accuracy is independent of spacecraft distance from the Earth. Present techniques for determining the two spacecraft coordinates other than range measure angles and thus degrade with increasing spacecraft range. Thus navigation using X-ray pulsars will always be superior to present techniques in measuring these two coordinates for sufficiently distant spacecraft. At present, the break-even point occurs near the orbit of Jupiter. The Crab pulsar can also be used to obtain one transverse coordinate with an accuracy of ~ 20 km.

Position Determination vs. Navigation

“You Are Here” vs. “To Go From Point A to Point B”



Credit: NASA

Deep Space Navigation and Position Determination

$$\mathbf{r}_{PD} = f(t_{PD})$$

$$t_{PD} = t_{SSB} + t_{corr} - DDM/v^2 + \Delta_{R\odot} + \Delta_{S\odot} + \Delta_{E\odot}$$

$$\Delta_{R\odot} = -\mathbf{r} \cdot \hat{\mathbf{s}}/c$$

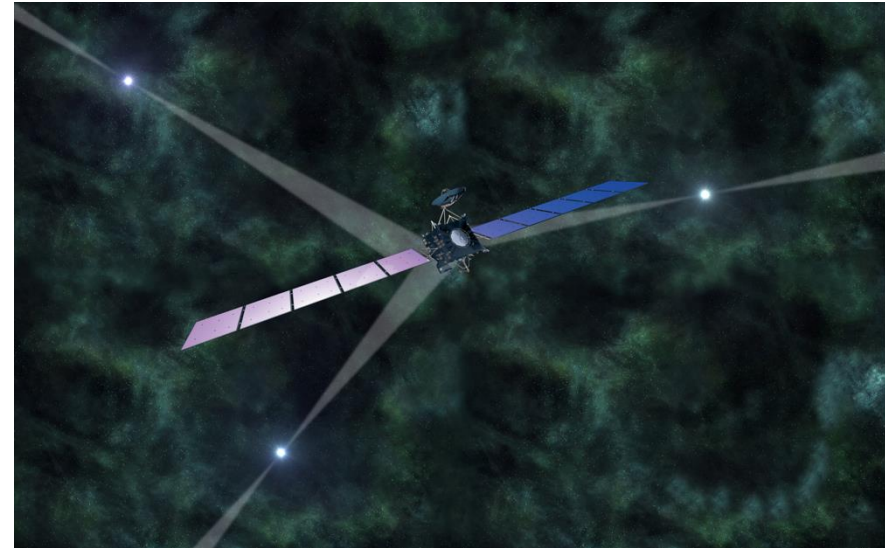
Lorimer & Kramer

$$\triangleright \sigma_{PD} = f(\sigma_{SSB}; \dots)$$

$$\sigma_{SSB} \sim 100 \text{ m}$$

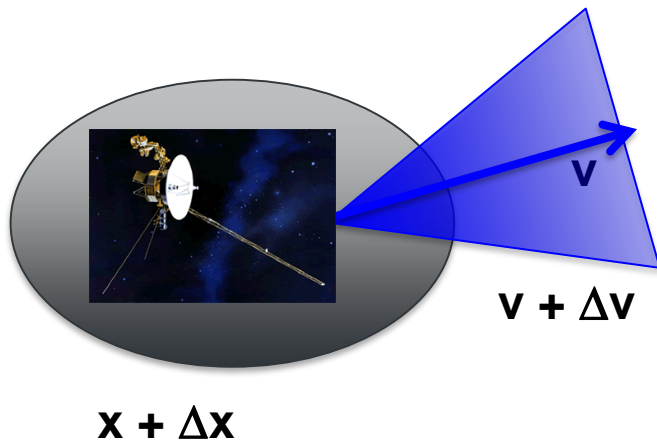
$$\sigma_{PD} \propto \sigma_{SSB}/\sqrt{N} \text{ ?}$$

$$\triangleright |\mathbf{v}| \sim 30 \text{ km/s}$$



Credit: MPE/W. Becker; ESA

Spacecraft Navigation



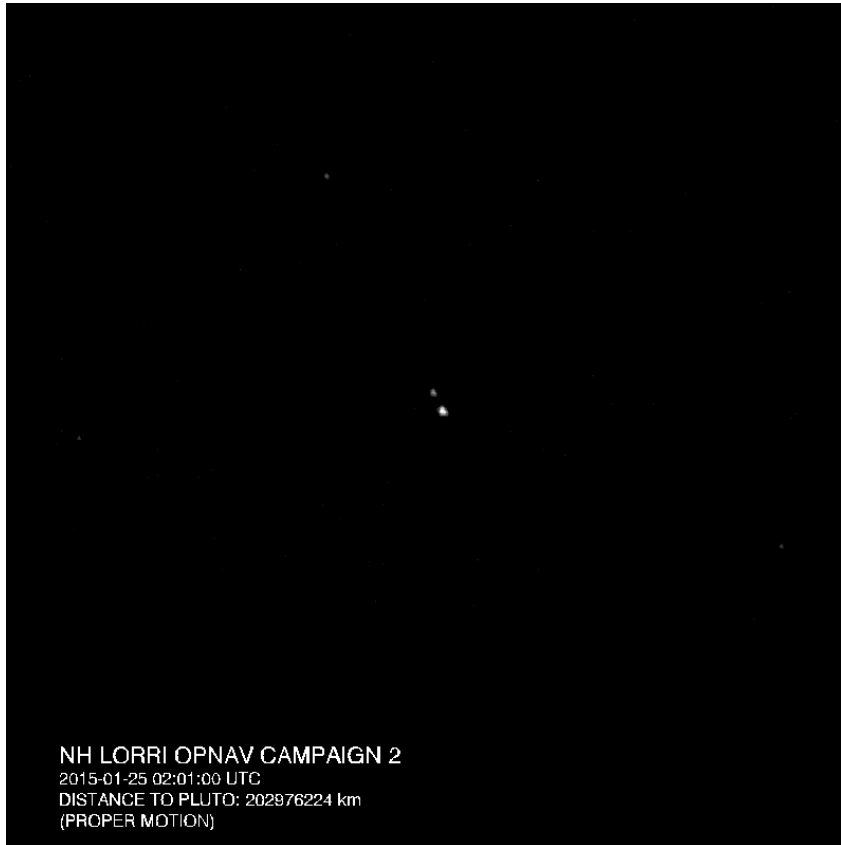
State-of-the-Art Navigation

Representative Values for General Context

- Quiet interplanetary cruise: $x \sim 10^8$ km, $v \sim$ few cm/s
- Delivery to Mars orbit insertion: ~ 10 km in B-plane (MRO)
- Delivery to Mars atmospheric entry: 0.21° in flight path angle (InSight)
- Mars orbit
 - $0.5 \times 20 \times 5$ m in RTN coordinates (MRO)
 - 5 day prediction of 1.5 km downtrack, 28 day prediction of ~ 200 km downtrack (MRO)
- Jupiter orbit
 - Knowledge of $0.1 \times 10 \times 2$ km (RTN) at perijove (Juno)
 - Delivery to Jupiter orbit insertion: ~ 100 km (Juno)
- Delivery to Titan flybys: < 1 km (*Cassini*)
- Delivery to Saturn icy moon flybys: < 2 km (*Cassini*)
- Delivery to Pluto flyby: ~ 100 km (NH Pluto)
- Small body orbit: < 50 m (Rosetta)
- Small body landing: < 25 m (OSIRIS-Rex)

Optical Navigation

New Horizons approaching Pluto



Credit: NASA/Johns Hopkins University
Applied Physics Laboratory/Southwest
Research Institute

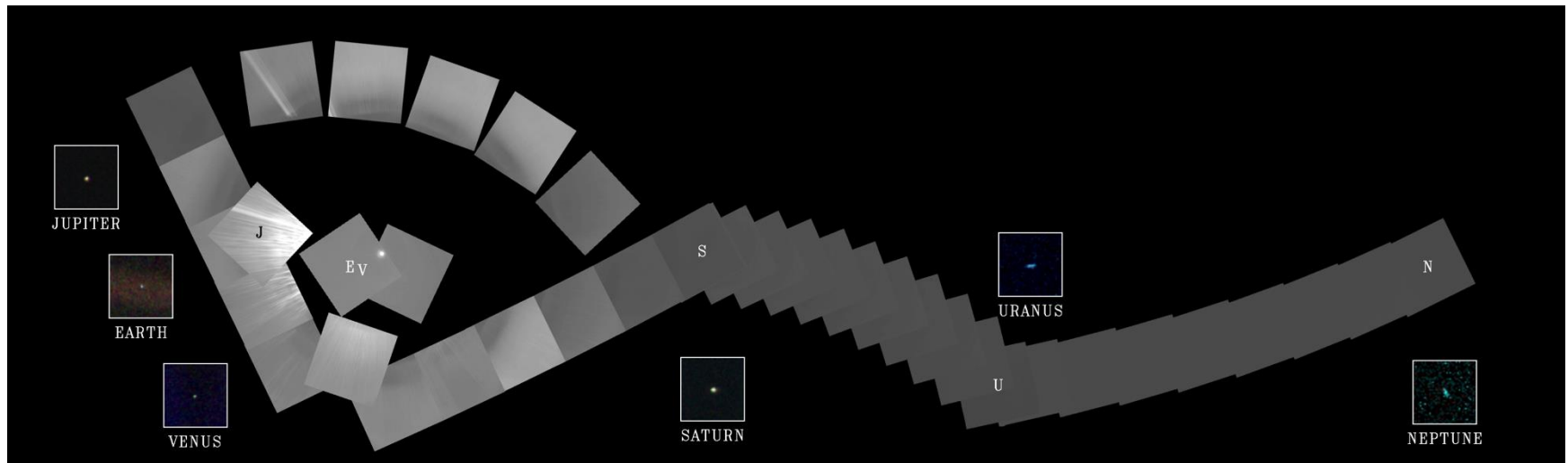
~~Cochrane~~ approaching TRAPPIST-1 Juno approaching Jupiter



Credit: NASA/JPL

Summary

- **Solar system barycenter is critical element for pulsar timing and GW studies**
- **Little spacecraft navigation need for improved determination of barycenter (~ 100 m)**
- **GW study or barycenter determination? Probably cannot do both with current census**
- **Implications for pulsar-based position determination**





Backup



Jet Propulsion Laboratory
California Institute of Technology

Mars VLBI Data

Dominant Error Source Mars Spacecraft VLBI on Goldstone-Madrid Baseline

